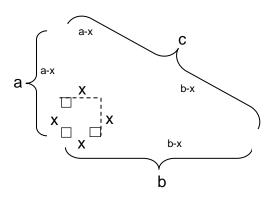
- 1. Let P = 1!2!3!!!n = n! and let S = 1 + 2 + 3 + E + n, where n is a positive integer.
 - (a) Prove that ifn is odd, therSdividesP exactly.
 - (b) Prove that the converse of part (a) true.
- 2. Let 1 2 3 7

1. (a) If n is odd, them = 2k + 1 where k is a positive integer. Then

$$\frac{P}{S} = \frac{1!2!3!!!(2k+1)}{1+2+3+...+(2k+1)} = \frac{(2k+1)!}{\frac{1}{2}(2k+1)(2k+2)} = \frac{(2k+1)!}{(2k+1)(k+1)}$$

For every<u>odd</u> integer k, $ak^2 + bk$ is the sum of two odd integers, and therefore $ak^2 + bk$ is an even integer. Sto(k) = ak + bk) + c



Next consider either the remaining two circles